

Reciprocal Lattice :-

Every crystal is associated with 2 type of lattices :-

- i) direct lattice
- ii) Reciprocal lattice

Need of Reciprocal lattice :-

In direct lattice, lattice points are arranged according to their position.

In Reciprocal lattice, lattice points are arranged according to their wave vector ($\vec{k}$) or momentum ($\hbar k$).

Hence direct lattice is defined in Position space.

Reciprocal " " " " Momentum space or

Fourier space.

They are inversely related i.e. position & mom. are conjugate of each other.

→ direct lattice has the unit of length.

→ Reciprocal " " " " $[\text{length}]^{-1}$

Wave vector is no. of waves per unit wave length. It tells, in which dirⁿ wave is propagating i.e.

$$k = \frac{2\pi}{\lambda}$$

✓ Potⁿ Energy in position space.

✓ K.E. in Mom. space.

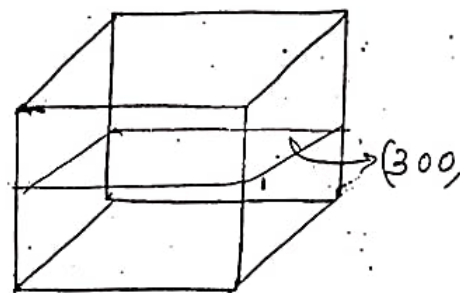
Total Energy is Conserved, i.e. K.E. & P.E. are inversely related. { K.E. ↓ as much P.E. ↑ }

If e^- is completely free then it will have K.E. only.

Reasons for need of Rec. Lattice :-

- It is difficult to visualize the crystal plane as order of the plane increases.

As $hkl \uparrow$, $d_{hkl} \downarrow$
 e.g. (300) plane $\rightarrow$ difficult to visualize.



In Reciprocal lattice, each plane is represented by its normal.
 & length of the normal is inversely proportional to interplanar spacing.

$\Rightarrow$ So smaller the " " , larger is the length of the normal.

$\Rightarrow$ Plane near in direct lattice will be far away in reci. lattice.

$\Rightarrow$ Every physical property of crystal is periodic.

To calculate e^- concentration (e^- conc. follow periodic prop)

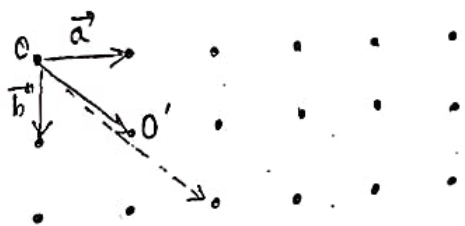
A funcⁿ is given $n(r) = n(r+a)$

To calculate e^- conc., we need to expand this funcⁿ & to expand periodic funcⁿ, we need Fourier series. & Fourier series is the concept of Fourier space or reci space.

* Every physical property of crystal is periodic like e^- conc. & magnetic moment.

* Fourier transform of direct lattice is reciprocal lattice, & Inverse " " " Reci. " " direct "

In 2 dim. direct lattice, there are 2 vectors $\vec{a}$ & $\vec{b}$.



To move from O to O' , we use

Translation Vector.

It is called Lattice Translation.

The vector joining 2 Lattice points is called Lattice Translation vectors.

$$\vec{T} = \vec{a} + \vec{b}$$

In general

$$\vec{T} = n_1 \vec{a} + n_2 \vec{b} + n_3 \vec{c}$$

It is defining in direct lattice only.

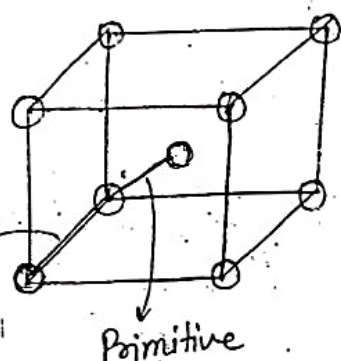
Where, a, b, c are Primitive direct lattice vectors.

bcz they are joining nearest lattice (points) vectors.

If they join far lattice points then these vectors will be non-primitive.

B.C.C.

Non-primitive
lattice
vector.



B.C.C. is 1 basis structure.

Lattice parameter $\rightarrow$ joining 1st
near neighbour.

Here, lattice vector connect non-
nearest lattice points. $\therefore$ Non-primitive

In Reciprocal lattice, $\vec{A}', \vec{B}', \vec{C}'$ are the primitive
Reciprocal lattice vectors.

$$\vec{A}' = \frac{2\pi (\vec{b}' \times \vec{c}')}{\vec{a}' \cdot (\vec{b}' \times \vec{c}')}$$

$$\vec{B}' = \frac{2\pi (\vec{c}' \times \vec{a}')}{\vec{a}' \cdot (\vec{b}' \times \vec{c}')}$$

$$\vec{C}' = \frac{2\pi (\vec{a}' \times \vec{b}')}{\vec{a}' \cdot (\vec{b}' \times \vec{c}')}$$

Reciprocal lattice vector

$$\vec{G}' = h \vec{A}' + k \vec{B}' + l \vec{C}'$$

$$e^{i \vec{a} \cdot \vec{T}} = 1$$

$$\vec{G}' \cdot \vec{T} = 2\pi n$$

, $n \rightarrow$ some integer

$$n = 0, 1, 2, \dots$$